



Maths – How do we learn?

Learning, Teaching and Supporting in Maths

Calculation Strategies

We teach 4 strands of Maths

- ▶ Number
- ▶ Shape, Space and Measures
- ▶ Data Handling
- ▶ Using and Applying Maths

Using and Applying Maths happens in all of the strands, as well as in other lessons, such as Science.



Number

Over the next 2 workshops, we will focus on the four operations (+, x and then -, ÷)

- ▶ Today we are focusing on + and x
- ▶ We will work through the Calculation Policy
- ▶ We will also look at some of the resources we use to teach number in School.
- ▶ As well as how you can help at home!



Maths

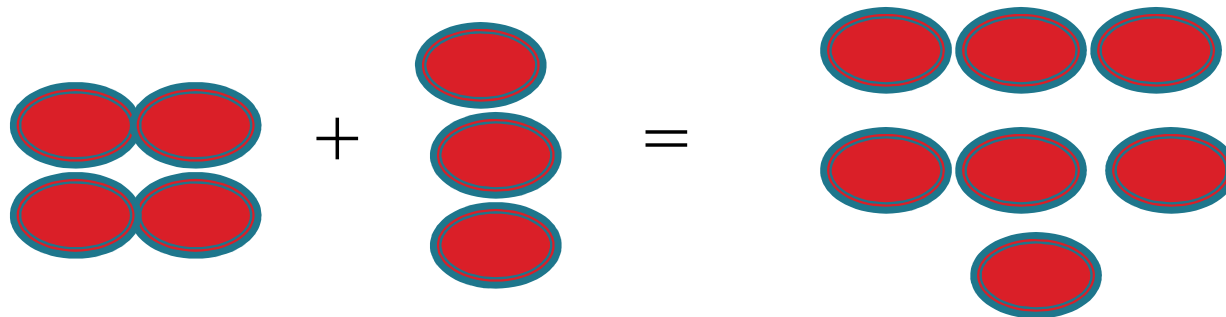
How do we learn Addition?



Adding– Stage 1

Children begin in EYFS and Key Stage 1 by adding real objects, such as cubes. They combine sets and count the total.

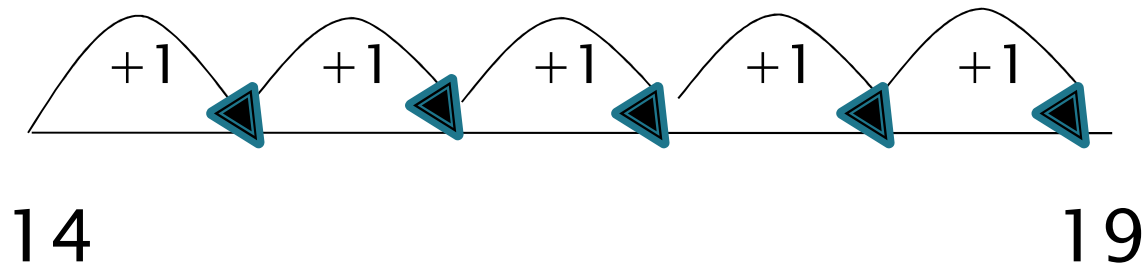
Count 4 cakes. Count 3 cakes. How many altogether?



Adding- Stage 2

We then move on to using number lines and counting up in ones.

$$14 + 5 = 19$$



Partitioning- Stage 3


Next we learn to partition - split the number into tens and units - to add.

What is $72 + 14$?

T	U
70	2
10	4

$$70 + 10 = 80$$

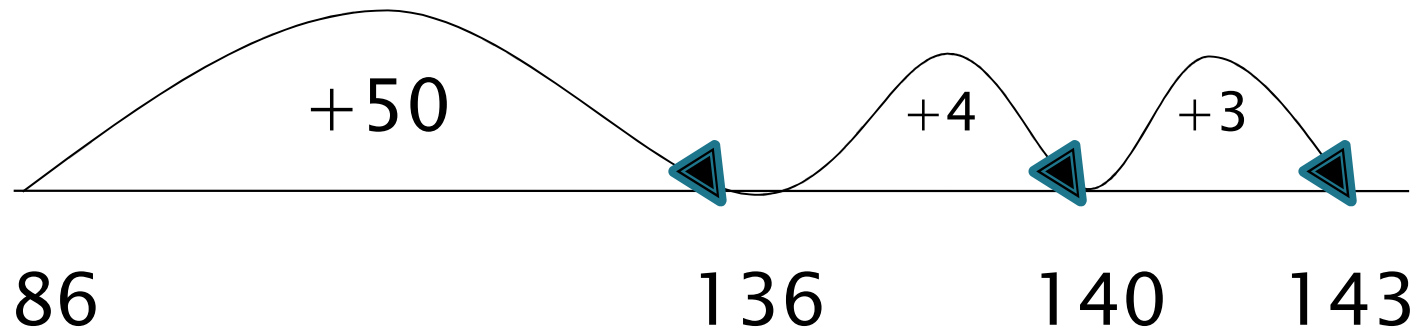
$$2 + 4 = 6$$

$$80 + 6 = 86$$


Adding by Partitioning

Now we can add by partitioning -

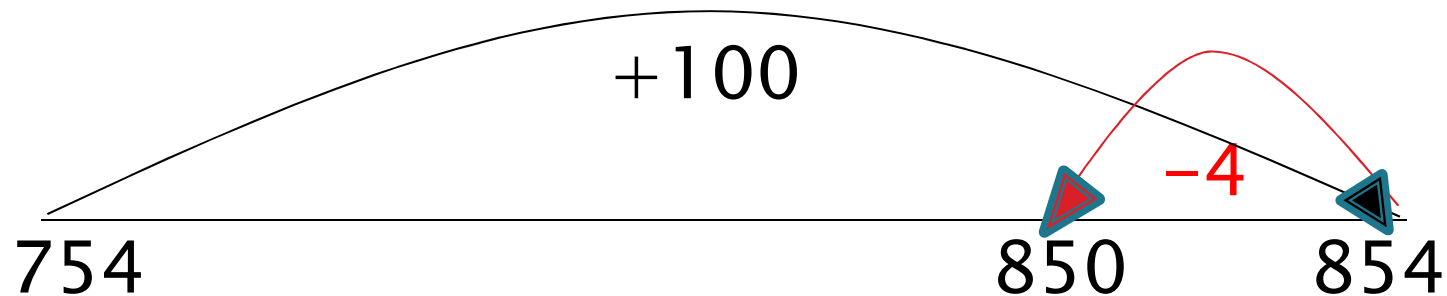
$$86 + 57 =$$



Adding by Partitioning

Or by rounding then adjusting

754 + 96 (rounding and adjusting)



Column Addition– Stage 4

Expanded method moving to compact with carryings 10s only

$$\begin{array}{r} \text{HTU} \\ 647 \\ + \underline{334} \\ 11 \\ 70 \\ \underline{900} \\ \underline{981} \end{array} \quad \text{and} \quad \begin{array}{r} \text{HTU} \\ 647 \\ + \underline{334} \\ \underline{981} \\ 1 \end{array}$$



Column Addition– Stage 5

Refine compact method with carrying under the line

$$\begin{array}{r} \text{HTU} \\ 597 \\ + \underline{475} \\ \hline 1072 \\ \text{1 1} \end{array}$$

and

$$\begin{array}{r} \text{ThHTU} \\ 7648 \\ + \underline{1486} \\ \hline 9134 \\ \text{1 1 1} \end{array}$$



Decimal Addition– Stage 6

Importance of lining up with decimal point

$$\begin{array}{r} \text{TU.t} \\ 59.7 \\ + \quad \underline{4.1} \\ \hline \underline{63.8} \\ 1 \end{array}$$

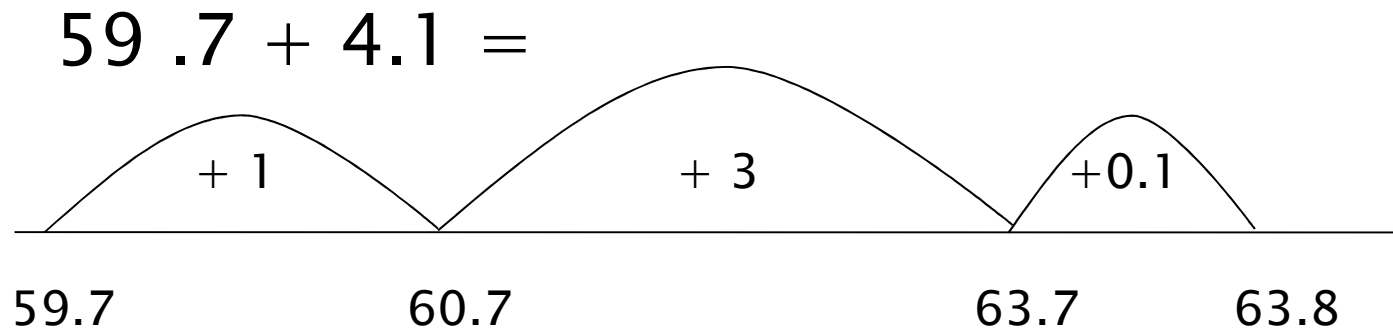
and

$$\begin{array}{r} \text{HTU.t h} \\ 137.42 \\ + \quad \underline{14.87} \\ \hline \underline{152.29} \\ 1 \quad 1 \end{array}$$



Decimal Addition– Stage 6

A number line can also be used for adding decimals by partitioning and counting on to the next whole digit/number



So $59.7 + 4.1 = 63.8$



Decimal Addition– Stage 7

Importance of lining up with decimal point and adding place holders if different number of digits


$$\begin{array}{r} \text{TU.t} \\ 59.73 \\ + \quad \underline{4.10} \\ \hline \underline{63.83} \\ 1 \end{array}$$

and

$$\begin{array}{r} \text{HTU.t h} \\ 137.20 \\ + \quad \underline{14.87} \\ \hline \underline{152.08} \\ 1 \quad 1 \end{array}$$



Finally ...


- ▶ Importance of working through the stages and not expecting it to be linked to year group– need to understand how/why it works and not just learn the method!
 - ▶ Children need to choose appropriate method for the problem so if its $2996 + 1993$ then column addition will work but would rounding and adjusting be more efficient?
 - ▶ We encourage them to choose the most effective and efficient method so number line with decimals could be more accurate
 - ▶ Any questions?
- 

Resources for Addition

Maths Caddies:

- ▶ Mini number grid– 100 square
- ▶ Digit cards
- ▶ Number fans
- ▶ Mini counting sticks

Classroom resources:

- ▶ Cubes
 - ▶ Objects for counting
 - ▶ Bead strings
 - ▶ Dienes materials
 - ▶ Money
- 

Maths

How do we learn Multiplication?



Counting and doubling– Stage 1

Using objects to double a number, counting in 10s.

Double 2 =

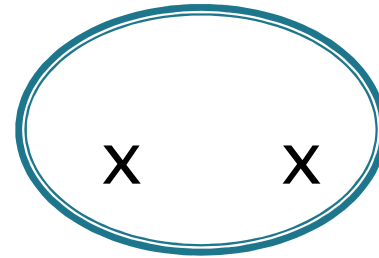
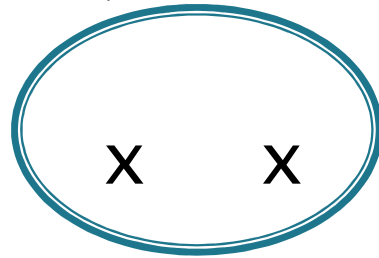
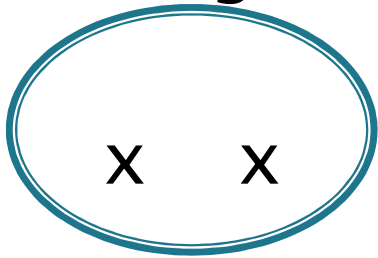


Repeated addition– Stage 2

Understand x is repeated +

$$4 \times 2 = 4 \text{ lots of } 2 \text{ so } 2 + 2 + 2 + 2 = 8$$

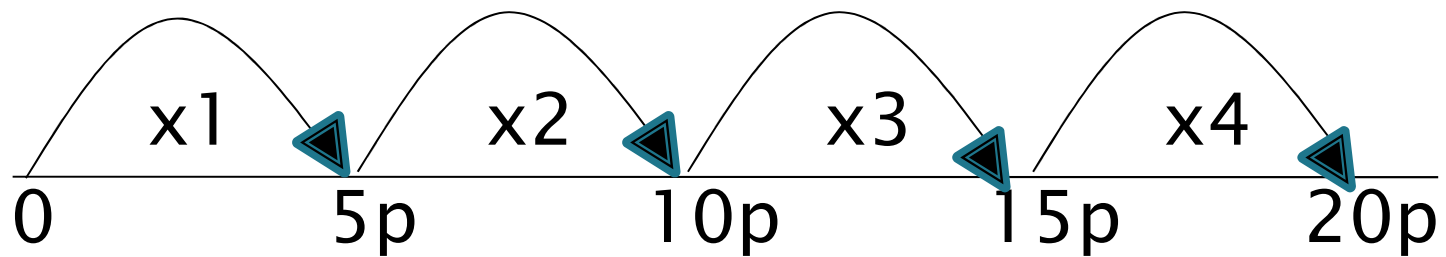
Counting in 2s, 5s, 10s



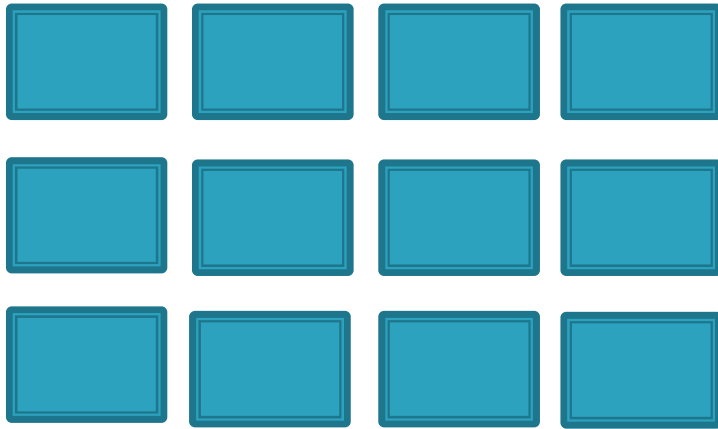
Number lines– Stage 3

Now we use the number line for repeated addition.

I have 4 5p coins, how much is that?



Multiplying using arrays



$$3 \times 4 = 12$$

3 rows of 4

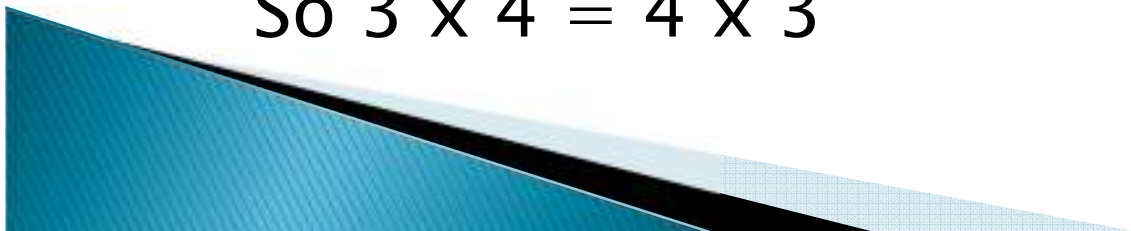
3 lots of 4

$$4 \times 3 = 12$$

4 columns of 3, 4 lots of 3

Commutative- can be done in any order

$$\text{So } 3 \times 4 = 4 \times 3$$



The Grid Method– Stage 4

We can partition to multiply using a grid

$$72 \times 8 =$$

x	70	2
8	560	16

Then add up each row so 560

$$\begin{array}{r} + \quad 16 \\ \hline 576 \end{array}$$



Grid Method– Stage 5

This method can also be used for HTU x U and TU x TU

$$72 \times 38 = \begin{array}{|c|c|c|} \hline x & 70 & 2 \\ \hline 30 & 2100 & 60 \\ \hline 8 & 560 & 16 \\ \hline \end{array} = 2160 + \underline{576} = \underline{2736}$$

Then add up all the numbers



Column Method for x- Stage 6

Expanded column method

$$\begin{array}{r} 346 \\ \times \quad \underline{8} \\ 48 \quad (8 \times 6) \\ 320 \quad (8 \times 40) \\ + \quad \underline{2400} \quad (8 \times 300) \\ \underline{2768} \end{array}$$



Short x- Stage 7

Start by multiplying by the units and work across from right to left- carrying at the bottom where necessary!

$$\begin{array}{r} \\ x \\ \hline 2768 \\ \hline \\ \\ \end{array}$$

$$\begin{array}{r} \\ x \\ \hline 2125 \quad (5 \times 425) \\ \\ + \\ \\ \\ \\ \hline 12750 \quad (30 \times 425) \\ \\ \\ \\ \hline 14875 \end{array}$$



Also ...

- ▶ Importance of working through the stages and not expecting it to be linked to year group– need to understand how/why it works and not just learn the method!
- ▶ Only move onto long/short \times when ready as grid method is effective although not as efficient
- ▶ Use of number line to count on in groups can also be effective for larger numbers and decimals




Resources for Multiplying

Maths Caddies:

- ▶ Mini counting sticks
- ▶ Number cards
- ▶ Multiplication square
- ▶ Place value sliders

Classroom resources:

- ▶ Cubes
 - ▶ Dienes materials
 - ▶ Number lines
 - ▶ Money
- 

And Finally...

It is vitally important that children understand the order and value of numbers in context.

There are many opportunities for counting, adding and multiplying in real life – please use them!

If you have any questions then don't hesitate to ask!

